

Teaching for Mastery

Calculation Policy

Written by Amy Marriott

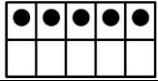
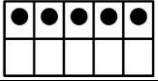
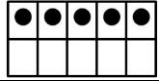
Reviewed July 2024

Next review date July 2026



Progression in the use of manipulatives to support learning **USE IT!**

Foundation	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Real-life objects	Real-life objects	Real-life objects	Real-life objects	Real-life objects	Real-life objects	Real-life objects
0 – 9 digit cards	0 – 9 digit cards	0 – 9 digit cards	0 – 9 digit cards	0 – 9 digit cards	0 – 9 digit cards	0 – 9 digit cards
Number track to 10	Number line to 20	Number line to 100	Number line to 100	Number line including negative numbers	Number line including negative numbers	Number line including negative numbers

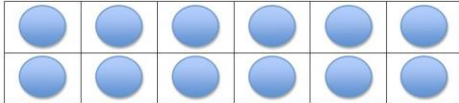
Numbered counting stick	Counting stick	Counting stick	Counting stick	Counting stick	Counting stick	Counting stick
Tens frame 	Tens frame 	Tens frame 				
	Place value charts – Tens and ones	Place value charts – Hundreds, tens and ones	Place value charts – Thousands, hundreds, tens and ones	Place value charts – Ten thousands, thousands, hundreds, tens, ones and tenths	Place value charts to a million and three decimal places	Place value charts to 10 million and three decimal places
Interlocking cubes - Use one colour to represent one amount	Interlocking cubes - Use one colour to represent one amount	Dienes	Dienes	Dienes	Dienes	Dienes
			Place value counters	Place value counters	Place value counters	Place value counters
	Place value arrow cards – tens and ones	Place value arrow cards – tens and ones	Place value arrow cards – H, T, O	Place value arrow cards – Th, H, T, O	Place value arrow cards	Place value arrow cards
Part-part-whole mat	Part-part-whole mat	Part-part-whole mat	Part-part-whole model	Part-part-whole model	Part-part-whole model	Part-part-whole model
Bar model with reallife objects	Bar model with real life objects/pictorial objects/representative objects eg. counters	Bar model with counters /Dienes progressing to numbers	Bar model with numbers	Bar model with numbers	Bar model with numbers	Bar model with numbers
Bead strings – ten	Bead strings - twenty	Bead strings - hundred	Bead strings - hundred	Bead strings - hundred	Bead strings - hundred	Bead strings - hundred
Numicon shapes	Numicon shapes	Numicon shapes	Numicon shapes	Numicon shapes	Numicon shapes	Numicon shapes
			Cuisenaire rods	Cuisenaire rods	Cuisenaire rods	Cuisenaire rods
Double sided counters	Double sided counters	Double sided counters	Double sided counters	Double sided counters	Double sided counters	Double sided counters
Multilink – use one colour to model an amount	Multilink – use one colour to model an amount	Multilink – use one colour to model an amount	Multilink – use one colour to model an amount	Multilink – use one colour to model an amount	Multilink – use one colour to model an amount	Multilink – use one colour to model an amount

Maths Working Wall – **DISPLAY IT (CPA representations of the questions)**

Build it!

Use a real-life representation of the concept which children can see, touch and feel.



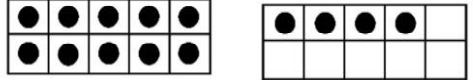
Draw it!	Show a pictorial representation of the concept.	
Solve it!	Show the mathematical representation of the concept.	$6 \times 2 = 12$ $12 \div 2 = 6$ $2 \times 6 = 12$ $12 \div 6 = 2$ Factors of 12 are: 1, 2, 3, 4, 6 and 12
Practise it!	Encourage children to practice the concept. Interactive opportunity – ask children to respond to questions, encourage them to add what they know, leave homework for children to take to master the concept.	$1 \times 2 = 2$ $2 \times 2 = 4$ $3 \times 2 = 6$ etc.
Challenge it!	Set a challenge to be solved. Interactive opportunity – leave real-life objects or manipulatives for children to use to help solve the challenge.	How many different ways can 12 eggs be arranged into arrays? What if you try 24 eggs?
Say it!	Use vocabulary related to the concept	Multiply, times, repeated addition, array, divide, group, multiples, factors

Classroom Visual Prompts – SEE IT! Enable Tables

Foundation	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Big focus 10	Big focus 20	Big focus 100				

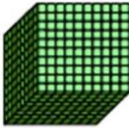



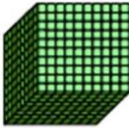



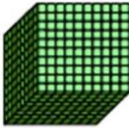



Numicon number line with Numicon shapes	Numicon number line with Numicon shapes	Numicon number line	Fractions number line	Fractions and decimals number line	Fractions, decimals and percentages number line	Fractions, decimals and percentages number line
	Odd and even numbers	Odd and even numbers			Prime, square and cube numbers	Prime, square and cube numbers
	Number pairs totalling 10 Number pairs totalling 20	Number pairs totalling 10 Multiples of 10 totalling 100	Number pairs totalling 10 Multiples of 10 totalling 100			
0 – 10 number line / track	0 -20 number line	0 – 100 number line	Number line to 100	Number line including negative numbers	Number line including negative numbers	Number line including negative numbers
	100 square	100 square	100 square	100 square		
Number names from 0 - 10	Number names from 0 - 20	Number names from 0 – 100	Number names from 0 - 1000	Number names to one million	Number names to tens of million	Number names to tens of millions
Real coins Large coins	Real coins Large coins	Real coins Large coins	Real coins Large coins	Real coins Large coins	Real coins Large coins	Real coins Large coins
	1, 2, 5 and 10 times tables	2, 3, 4, 5 and 10 times tables	All times tables up to 12 x 12	All times tables up to 12 x 12	All times tables up to 12 x 12	All times tables up to 12 x 12
			Roman numerals	Roman numerals	Roman numerals	Roman numerals
		< , > and = signs	< , > and = signs	< , > and = signs	< , > and = signs	< , > and = signs
Real-life / pictorial fractions	Real-life / pictorial fractions	Fractions including fraction number line/wall	Fractions including fraction number line/wall	Fractions including fraction number line/wall	Fractions, decimals and percentages including fraction number line/wall	Fractions, decimals and percentages including fraction number line/wall
						BIDMAS
2d and 3d shapes	2d and 3d shapes	2d and 3d shapes	2d and 3d shapes	2d and 3d shapes	2d and 3d shapes	2D and 3D shapes

Progression in the teaching of place value

Foundation	Year 1	Year 2	Year 3 onwards
Understanding ten	Understanding numbers up to 20	Understanding numbers up to one hundred	Understanding numbers up to one thousand
<p>A TENS FRAME is a simple maths tool that helps children:</p> <ul style="list-style-type: none"> Keep track of counting See number relationships Learn addition to 10 	<p>'Ten' is the building block of our Base 10 numeration system. Young children can usually 'read' two-digit numbers long before they understand the effect the placement of each digit has on its numerical value. A child might be able to</p>	<p>Continue developing place value through the use of <i>tens frames</i>.</p> 	<p>Continue developing place value through the use of manipulatives.</p>

<ul style="list-style-type: none">Understand place value <p>Use tens frames flash cards daily to ensure children recognise amounts.</p> <p>Use empty tens frames to fill with counters to enable children to understand number relationships.</p> <p>Either fill the tens frame in pairs or in rows. In rows shows 5 as a benchmark. Children can easily see more than 5 or less.</p> <table border="1"><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr><tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr></table> <p>Setting the counters in pairs, naturally allows the children to see addition concepts.</p> <p>Include other visual images such as dice, cards, dominoes etc.</p> <div><table border="1"><tr><td>●</td><td>●</td><td>●</td></tr><tr><td>●</td><td>●</td><td> </td></tr></table><table border="1"><tr><td> </td><td> </td><td> </td><td>●</td><td>●</td></tr><tr><td> </td><td> </td><td> </td><td>●</td><td>●</td></tr></table><table border="1"><tr><td>5</td><td>♥</td><td>♥</td><td>♥</td></tr><tr><td> </td><td>♥</td><td> </td><td>♥</td></tr><tr><td>♥</td><td>♥</td><td>♥</td><td>5</td></tr></table><table border="1"><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr></table></div>	●	●	●	●	●						●	●	●	●	●					●	●				●	●	5	♥	♥	♥		♥		♥	♥	♥	♥	5	●	●	●	●	●	●	●	●	●	●	<p>correctly read 62 as sixty two and 26 as twenty-six, and even know which number is larger, without understanding why the numbers are of differing values.</p> <p>Ten-frames can provide a first step into understanding two-digit numbers simply by the introduction of a second frame. Placing the second frame to the right of the first frame, and later introducing numeral cards, will further assist the development of place value understanding.</p> <table border="1"><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr></table> <table border="1"><tr><td>●</td><td>●</td><td>●</td><td> </td><td> </td></tr><tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr></table> <div><table border="1"><tr><td>10</td></tr></table><table border="1"><tr><td>4</td></tr></table></div> <table border="1"><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr><tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr></table> <table border="1"><tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr><tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr></table> <div><table border="1"><tr><td>10</td></tr></table><table border="1"><tr><td>4</td></tr></table></div> <table 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Progression in the teaching of place value		
Year 4	Year 5	Year 6

Understanding numbers up to ten thousand	Understanding numbers up to one million including decimals	Understanding numbers beyond one million including decimals																																																																		
<p>Continue developing place value through the use of manipulatives.</p> <ul style="list-style-type: none">Place value arrow cardsPlace value countersDienes blocksPlace value charts <table><tr><th>thousands</th><th>hundreds</th><th>tens</th><th>ones</th></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td>1 1,000</td><td>2 200</td><td>4 40</td><td>7 7</td></tr></table>	thousands	hundreds	tens	ones					1 1,000	2 200	4 40	7 7	<p>Continue developing place value through the use of manipulatives.</p> <ul style="list-style-type: none">Place value arrow cardsPlace value counters (including decimal counters)Dienes blocksPlace value charts <table><tr><th colspan="3">MILLIONS</th><th colspan="3">THOUSANDS</th><th colspan="3">ONES</th></tr><tr><th>hundred millions</th><th>ten millions</th><th>millions</th><th>hundred thousands</th><th>ten thousands</th><th>thousands</th><th>hundreds</th><th>tens</th><th>ones</th></tr><tr><td>7</td><td>4</td><td>5</td><td>3</td><td>0</td><td>9</td><td>2</td><td>8</td><td>1</td></tr></table>	MILLIONS			THOUSANDS			ONES			hundred millions	ten millions	millions	hundred thousands	ten thousands	thousands	hundreds	tens	ones	7	4	5	3	0	9	2	8	1	<p>Continue developing place value through the use of manipulatives.</p> <ul style="list-style-type: none">Place value arrow cardsPlace value counters (including decimals counters)Dienes blocksPlace value charts <table><tr><th colspan="3">MILLIONS</th><th colspan="3">THOUSANDS</th><th colspan="3">ONES</th></tr><tr><th>hundred millions</th><th>ten millions</th><th>millions</th><th>hundred thousands</th><th>ten thousands</th><th>thousands</th><th>hundreds</th><th>tens</th><th>ones</th></tr><tr><td>7</td><td>4</td><td>5</td><td>3</td><td>0</td><td>9</td><td>2</td><td>8</td><td>1</td></tr></table>	MILLIONS			THOUSANDS			ONES			hundred millions	ten millions	millions	hundred thousands	ten thousands	thousands	hundreds	tens	ones	7	4	5	3	0	9	2	8	1
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TENS FRAME IDEAS

LIFE SIZE TEN FRAME	Create a life-size ten frame in the classroom and outdoor play area. Use counters, pennies, teddies, gingerbread men, children etc.
FLASH	Flash <i>ten frame</i> briefly and have children write the number on a whiteboard. Using whiteboards , rather than having children say the number, ensures that all children attempt to respond and allows the teacher to assess class progress. When the response is oral, not all child responses are audible. Encourage children to share the different strategies used to find the total number of dots for cards, “How did you see it?” This can be varied by asking children to write the number and draw the pattern they saw, or by having them build the number flashed on their own blank frame.
FLASH: ONE MORE	Once children are familiar with the basic patterns, and know them automatically, flash a 10 frame or dot card and ask them to name the number that is one more than the number flashed. Variation: ask children to give the number that is two more/one less/double/ten more than the number flashed.
I WISH I HAD TEN	Flash a dot card or ten frame showing 9 or less and say, “I wish I had 10”. Children respond with the part that is needed to make ten. The game can focus on a single whole, or the “wish I had” number can change each time. Variation: teacher flashes card and children write the complement of ten on individual whiteboards with dry erase markers.
I WISH I HAD 12	As above but children respond with how many more are needed to make twelve. Children should be confident in facts of 10 before this is attempted. For example to go from 8 to 12, they should realise they need 2 more to get to 10, then 2 more to 12. 2 and 2 is 4. Variation: Children draw an empty number line on their whiteboards to show the two jumps used to get to the target number.
1 MORE 1 LESS 10 MORE 10 LESS	The following four prompts are written on the board: one more one less ten more ten less The teacher flashes a dot or ten frame card as the ‘starting number’. The first child selects one prompt. For example, if the teacher flashes a card showing ‘5’ the first child might say, “one more than 5 is 6”, the second child might say, “ten more than 6 is 16”, and the third child might say, “one less than 16 is 15”. Continue until all children have had a turn.
TEEN FRAME FLASH (11-20)	Teen Frame Flash (11-20) Once children are subitizing <i>ten frame</i> patterns 0- 10, cards showing larger numbers (i.e. more than one ten frame) should be introduced. Use mental math sessions with the following key questions: How many? How many more than 10? As children become familiar with the 'teen' patterns introduce further questions to develop number relationships. <ul style="list-style-type: none"> • What is one more/two more than the number I flashed? • What is one less/two less than the number I flashed? • How far away is the number I flashed from twenty? • Double the number I flash. • What is the near Doubles fact? (i.e., if 15 is flashed, children answer 7+8)
MULTIPLES	Flash a <i>tens frame</i> and ask children to give you the product if the number you flash was multiplied by 2, 5 etc.

Progression in the teaching of calculations

	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition	Combining two parts to make a whole: part whole model. Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Column method – no regrouping.	Column method- regrouping. (up to 3 digits)	Column method- regrouping. (up to 4 digits)	Column method- regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method- regrouping. (Decimals- with different amounts of decimal places)
Subtraction	Taking away ones Counting back Find the difference Part whole model Make 10	Counting back Find the difference Part whole model Make 10 Column method- no regrouping	Column method with regrouping. (up to 3 digits)	Column method with regrouping. (up to 4 digits)	Column method with regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method with regrouping. (Decimals- with different amounts of decimal places)
Multiplication	Doubling Counting in multiples Arrays (with support)	Doubling Counting in multiples Repeated addition Arrays- showing commutative multiplication	Counting in multiples Repeated addition Arrays- showing commutative multiplication Grid method	Column multiplication (2 and 3 digit multiplied by 1 digit)	Column multiplication (up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication (multi digit up to 4 digits by a 2 digit number)
Division	Sharing objects into groups Division as grouping	Division as grouping Division within arrays	Division within arrays Division with a remainder Short division (2 digits by 1 digit- concrete and pictorial)	Division within arrays Division with a remainder Short division (up to 3 digits by 1 digit- concrete and pictorial)	Short division (up to 4 digits by a 1 digit number interpret remainders appropriately for the context)	Short division Long division (up to 4 digits by a 2 digit number- interpret remainders as whole numbers, fractions or round)

Progression in the teaching of calculations

ADD IT!

Objective and strategies

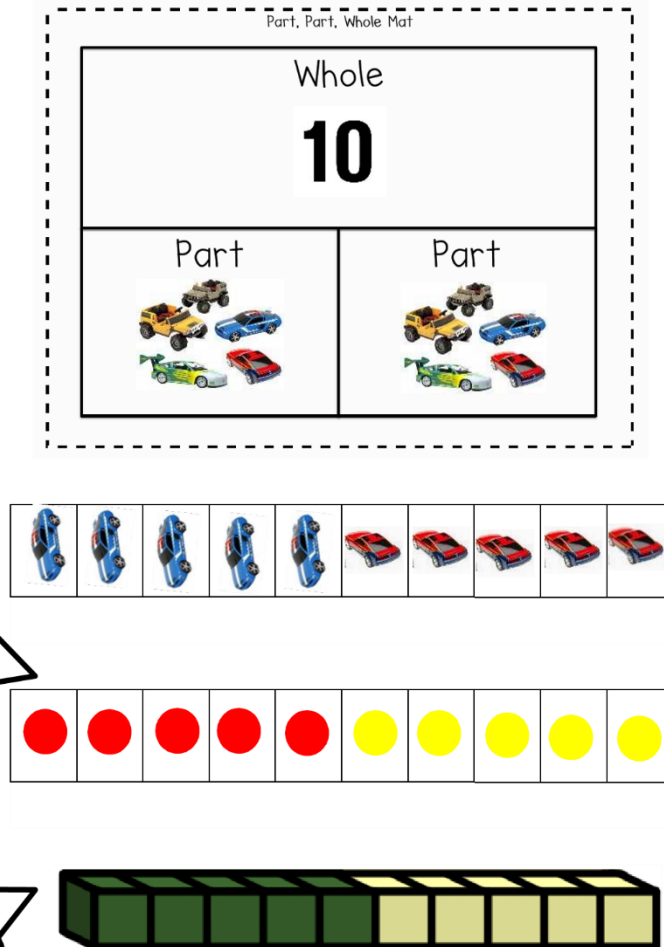
Combine two parts to make a whole model.

Part-part-whole model

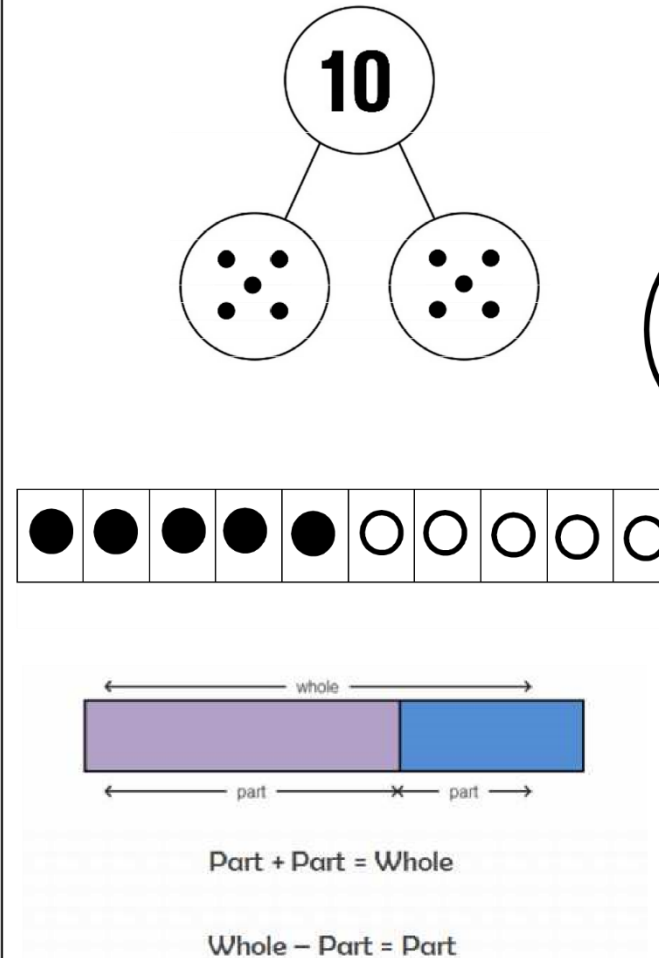
Teach the children that the cubes/counters represent the real-life objects.

Use cubes to add two numbers together as a group or in a bar.

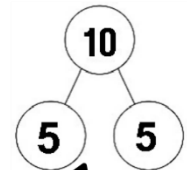
Concrete BUILD IT/USE IT!



Pictorial DRAW IT!



Abstract SOLVE IT!



Use the part-part whole diagram as shown above to move into the abstract.

$$5 + 5 = 10$$

$$10 = 5 + 5$$

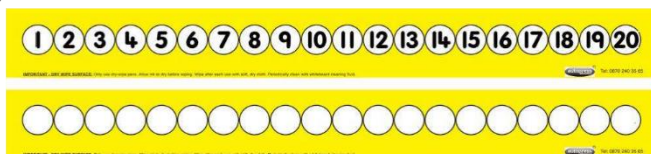
Use the term 'number sentence'.

Start at the larger number and count on

Start with the larger number on the bead string then count on 1 by 1 to find the



Use counters on a number track to count on.



$$7 + 4 = 11$$



Start at the larger number on the number line and count on in ones or in one jump to find the answer.

$$4 + 7 = 11$$

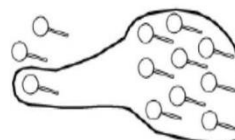
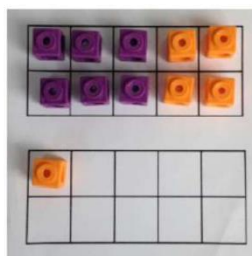
Place the larger number in your head and count on the smaller number to find your answer.

Regrouping to make 10.

Start with the bigger number and use the smaller number to make 10.



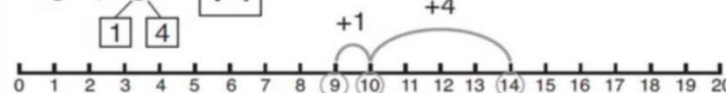
$$6 + 5 = 11$$



$$3 + 9 =$$

Use pictures or a number line. Regroup or partition the smaller number to make 10.

$$9 + 5 = 14$$



$$7 + 4 = 11$$

If I am at seven, how many more do I need to make 10. How many more do I add on now?

Adding three single digits.

Encourage children to use known facts.

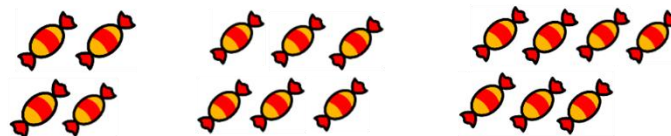
$$4 + 7 + 6 = 17$$

Put 4 and 6 together to make 10. Add on 7.



Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.

Add together three groups of objects. Draw a picture to recombine the groups to make 10.



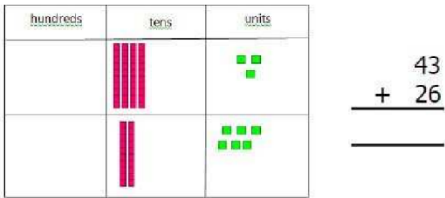
$$4 + 6 + 7 = 17$$

$$4 + 7 + 6 = 10 + 7$$

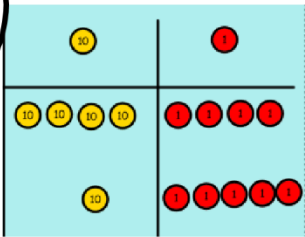
$$+ 10 = 17 +$$

Combine the two numbers that make 10 and then add on the remainder.

Column method-
no regrouping



Use Dienes to add
tens and ones
before moving on
to place value
counters.



After practically using the base 10 blocks and place value
counters, children can draw the Dienes to help them to
solve addition calculations.

hundreds	tens	ones
	////	□ □ □
	//	□ □ □ □ □ □
	6	9

After practically using Dienes, children can draw the ‘tens’
and ‘ones’.

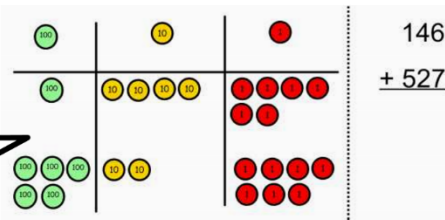
Calculations

21 + 42 =

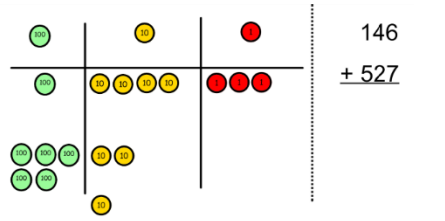
21
+ 42

Only select
numbers which
do not involve
regrouping.

Column method-
regrouping



Add up the
units and
exchange 10
ones for one
10 and so on.



Make both
numbers on a
place value grid.

This can also be done with Dienes to help children
clearly see that 10 ones equal 1 ten and 10 tens equal
100.

Continue using place value counters as children begin
to work with decimals.

If necessary children can draw a pictorial representation of
the columns and place value counters to further support
their learning and understanding.

hundreds	tens	ones
/	////	□ □ □ □ □ □
////	//	□ □ □ □ □ □ □
6	6	3
	1	

536
+ 85
621
11

As the children move on,
introduce decimals with the
same number of decimal
places.

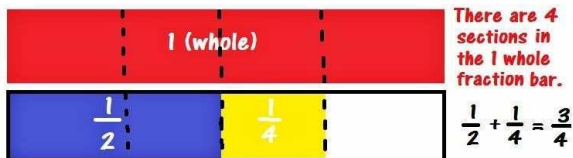
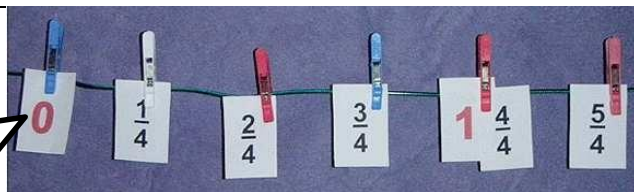
72.8
+ 54.6
127.4
11

Then move onto decimals
with a different number of
decimal places.

2 3 . 3 6 1
9 . 0 8 0
5 9 . 7 7 0
+ 1 . 3 0 0
9 3 . 5 1 1

Add fractions

Count in fraction steps using real objects and a number line.



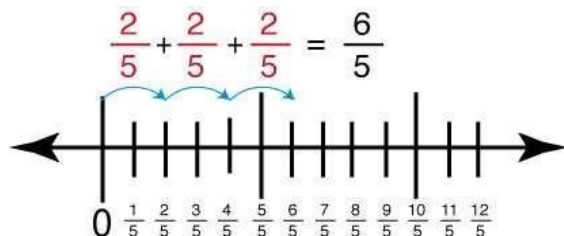
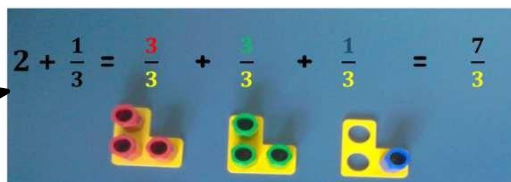
When I add the $\frac{1}{2}$ with the $\frac{1}{4}$ it matches the same space as three sections in the 'benchmark' one whole fraction bar.

LCD = least common denominator

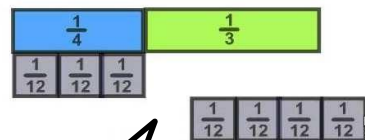
Find the LCD of 2 and 4 so you have a common denominator. Convert then add the numerators.

$$\begin{array}{r} \frac{1}{2} \times 2 = \frac{2}{4} \\ + \frac{1}{4} \times 1 = \frac{1}{4} \\ \hline \frac{3}{4} \end{array}$$

Use Numicon to add fractions.



$$\frac{1}{4} + \frac{1}{3}$$



Use the bar model to add fractions.





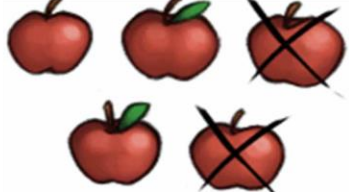


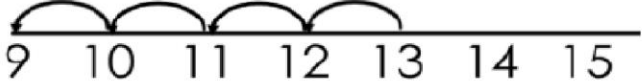
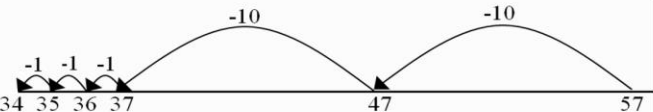
$$\frac{1}{4} + \frac{1}{3} =$$

$$\frac{1 \times 3}{4 \times 3} + \frac{1 \times 4}{3 \times 4}$$

$$\frac{3}{12} + \frac{4}{12} = \frac{7}{12}$$

Progression in Calculations Policy

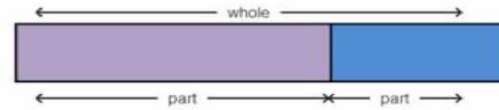
SUBTRACT IT!

Objective and strategies	Concrete BUILD IT/USE IT!	Pictorial DRAW IT!	Abstract SOLVE IT!
Taking away ones	<p>Use real-life physical objects, counters, cubes etc. to show how objects can be taken away.</p>  $6 - 2 = 4$   	<p>Cross out drawn objects to show what has been taken away.</p>  $5 - 2 = 3$	$4 = 6 - 2$ $18 - 3 = 15$ $8 - 2 = 6$
Counting back	<p>Make the larger number in the subtraction calculation. Move the beads along the bead string whilst counting backwards in ones.</p> <p>13 - 4</p>   <p>Use counters and move them away from the group whilst counting backwards.</p>	<p>Count back on a number line or number track</p>  <p>Start at the bigger number and count back the smaller number showing the jumps on the number line.</p> 	<p>Put 13 in your head, count back 4. What number are you at? Use your fingers to help.</p> <p>Children will need regular practice counting backwards.</p>

Use cubes to subtract a number from the bar.



Use the bar



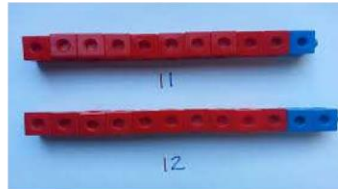
Part + Part = Whole

Whole - Part = Part

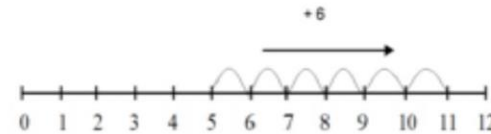
Find the difference

Compare amounts and objects to find the difference.

Use cubes to build towers or make bars to find the difference.

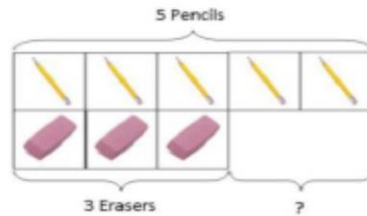


Count on to find the difference.



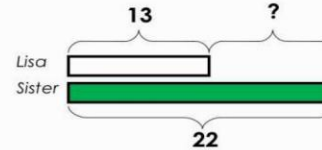
Hannah has 23 pencils, Helen has 15 pencils. Find the difference between the number of pencils.

Use basic bar models with items to find the difference.



Comparison Bar Models

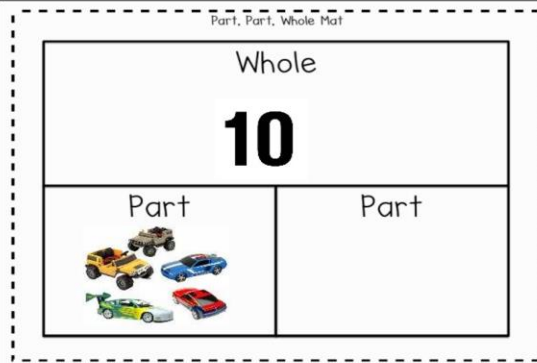
Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.



Draw bars to find the difference between two numbers.

Part-part-whole model

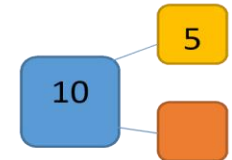
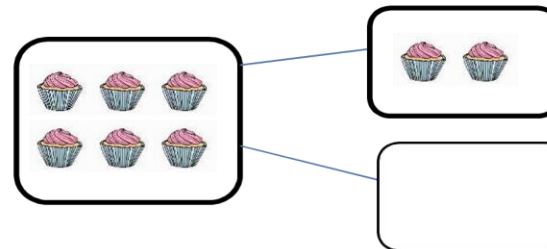
Link to addition-use the part whole model to help explain the inverse.



If 10 is the whole and 5 is one of the parts. What is the other part?

10 - 5 = or 10 - ? = 5

Use a pictorial representation of objects to show the part-part-whole model.

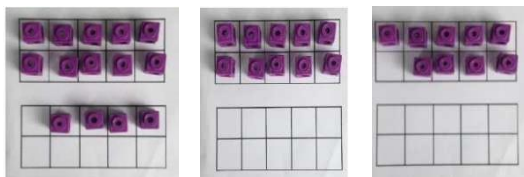


10 - 5 = 5 or 5 = 10 - ?

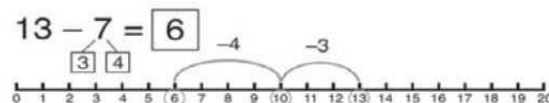
Move to using numbers with the part-part-whole model.

Make 10

$14 - 5 =$



Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.



Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.

$16 - 8 =$

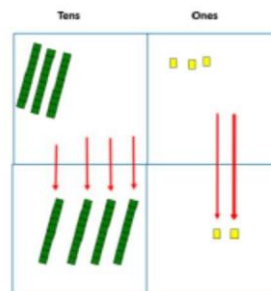
How many do we take off to reach the next 10?

How many do we have left to take off?

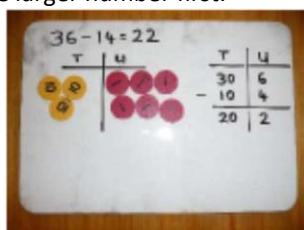
Column method without regrouping

$75 - 42 =$

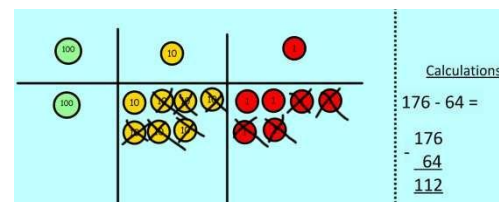
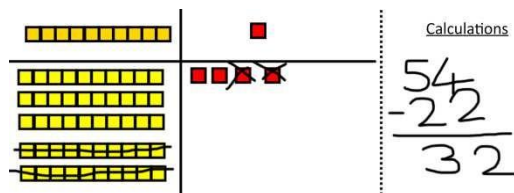
Use Dienes to make the bigger number then take the smaller number away.



Show how you partition numbers to subtract. Again make the larger number first.



Draw the Dienes or place value counters alongside the written calculation to help to show working.



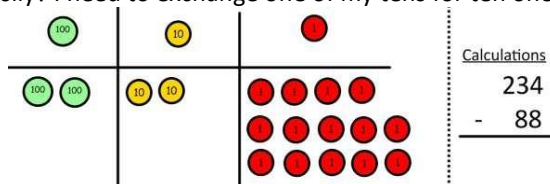
This will lead to a clear written column subtraction.

$$\begin{array}{r} 47 - 24 = 23 \\ - \quad 20 + 7 \\ \hline 20 + 3 \end{array}$$

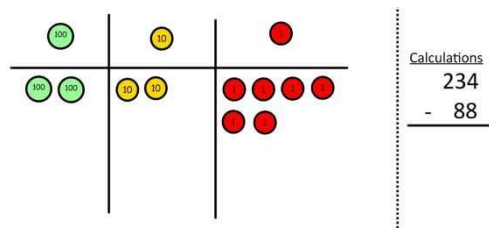
$$\begin{array}{r} 32 \\ - 12 \\ \hline 20 \end{array}$$

Column method with regrouping

Make the larger number with the Dienes or place value counters. Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.

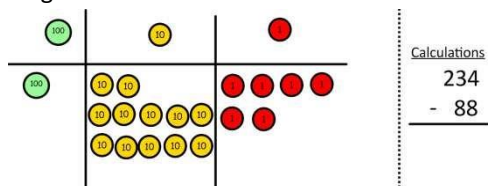


Now I can subtract my ones.

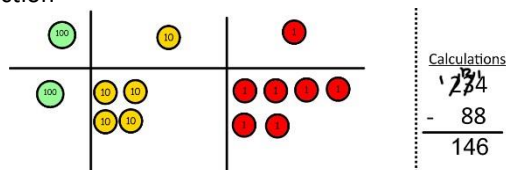


Now

look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.

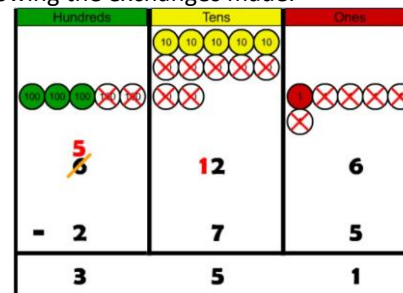


Now I can take away eight tens and complete my subtraction



Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

Draw the counters onto a place value grid and show what has been taken away by crossing the counters out as well as clearly showing the exchanges made.



When confident, children can find their own way to record the exchange/regrouping.

$$\begin{array}{r} 836 - 254 = 582 \\ \begin{array}{ccc} \text{H} & \text{T} & \text{U} \\ 800 & 30 & 6 \\ - 200 & 50 & 4 \\ \hline 500 & 80 & 2 \end{array} \end{array}$$

Children can start their formal written method by partitioning the number into clear place value columns.

$$\begin{array}{r} 728 - 582 = 146 \\ \begin{array}{ccc} \text{H} & \text{T} & \text{U} \\ 700 & 20 & 8 \\ - 500 & 80 & 2 \\ \hline 100 & 40 & 6 \end{array} \end{array}$$

Moving forward the children use a more compact method.

This will lead to an understanding of subtracting any number including decimals.

$$\begin{array}{r} \begin{array}{ccc} 5 & 12 & 1 \\ 2 & 6 & 3 \\ - 2 & 6 & 5 \\ \hline 2 & 3 & 6 \end{array} \end{array}$$

Subtract fractions

The cake has been divided into five slices. Each part is one fifth of the whole cake.

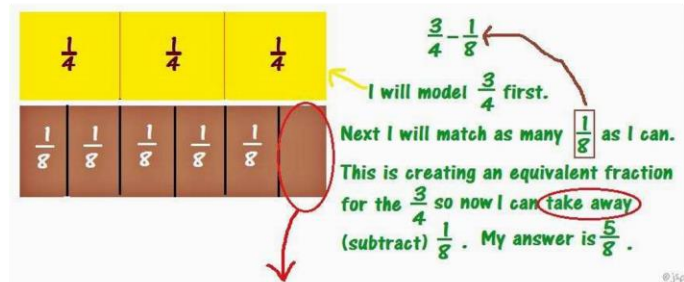


If there are five fifths and I eat one fifth, what fraction of the cake is left?

Draw a bar model to represent the cake.



Progress onto subtracting fractions with different denominators.



$$\frac{5}{5} - \frac{1}{5} = \frac{4}{5}$$

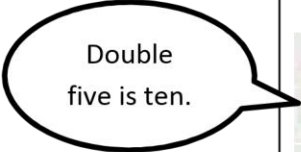


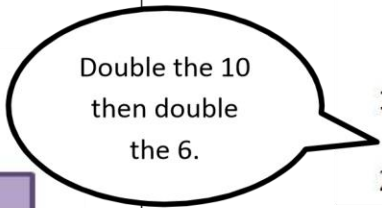
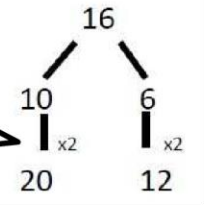
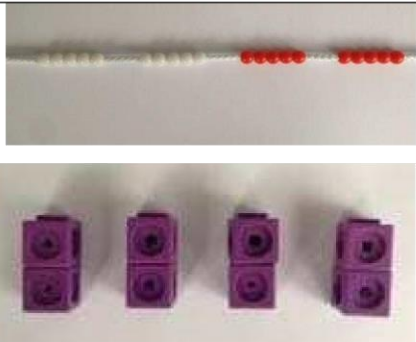
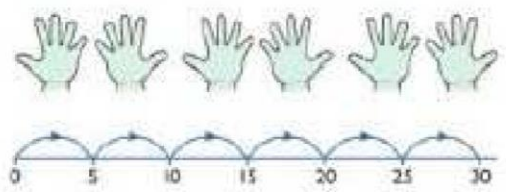
$$\frac{3}{4} - \frac{1}{8} =$$

$$\frac{3 \times 2}{4 \times 2} - \frac{1}{8}$$

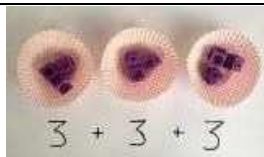
$$\frac{6}{8} - \frac{1}{8} = \frac{5}{8}$$

Progression in Calculations Policy

MULTIPLY IT!

Objective and strategies	Concrete BUILD IT/USE IT!	Pictorial DRAW IT!	Abstract SOLVE IT!
Doubling 	Use practical activities to show how to double a number.  $5 \times 2 = 10$	Draw pictures to show how to double a number. Double 4 is 8  	Double 16  Partition a number and then double each part before recombining it back together. Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Counting in multiples	 Count in multiples supported by concrete objects in equal groups.	 Use a number line or pictures to continue support in counting in multiples.	

Repeated addition

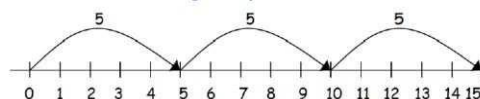


Use different objects to add equal groups.

There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?



2 add 2 add 2 equals 6



$$5 + 5 + 5 = 15$$

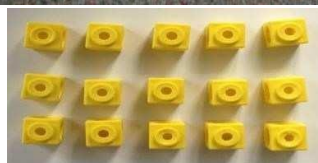
Write addition sentences to describe objects and pictures.



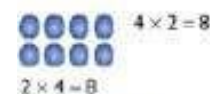
$$2 + 2 + 2 + 2 + 2 = 10$$

Arrays- showing commutative multiplication

Create arrays using counters/ cubes to show multiplication sentences.

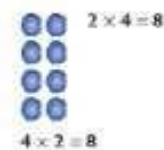


Draw arrays in different rotations to find **commutative** multiplication sentences.



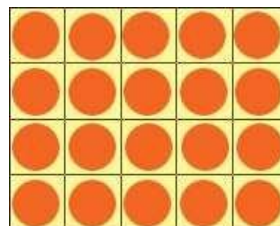
$$4 \times 2 = 8$$

$$2 \times 4 = 8$$



$$2 \times 4 = 8$$

$$4 \times 2 = 8$$



Link arrays to area of rectangles.

Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

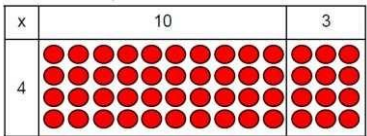
$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

$$3 \times 5 = 15$$

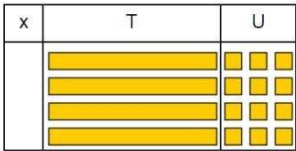
Grid Method

Show the link with arrays to first introduce the grid method.



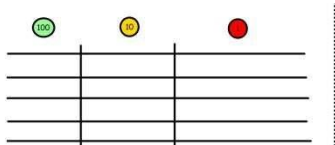
4 rows of
10 4 rows
of 3

Use Dienes to move towards a more compact method.



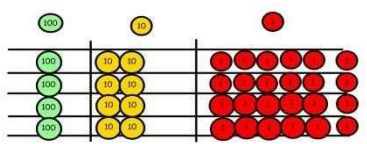
4 rows of 13

Use place value counters to show finding groups of a number eg. multiplying by 4 so we need 4 rows.



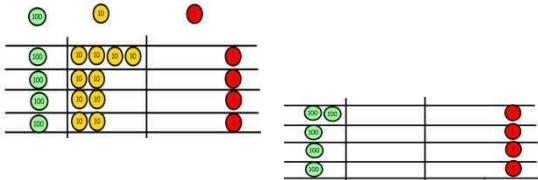
Calculations
4 x 126

Fill each row with 126.



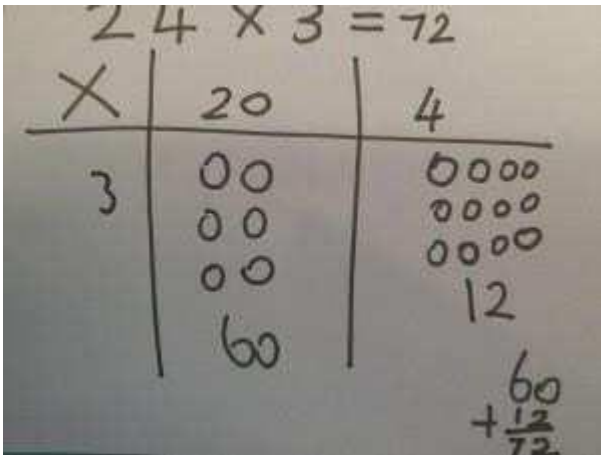
Calculations
4 x 126

Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

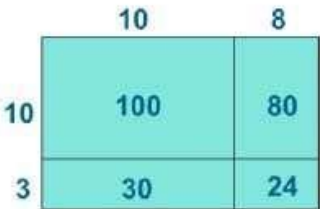


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

x	30	5
7	210	35

$$210 + 35 = 245$$

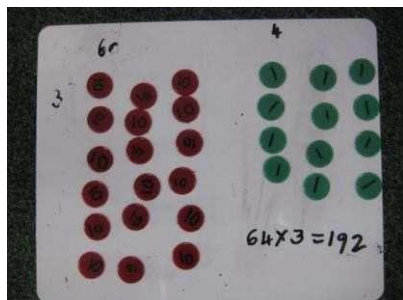
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



x	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

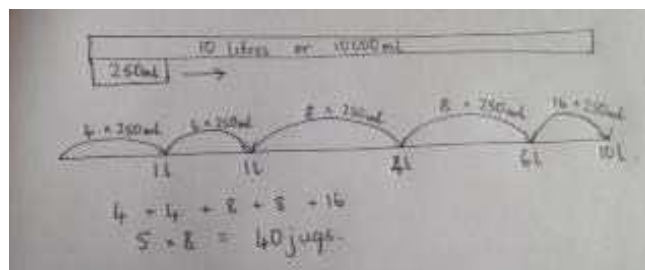
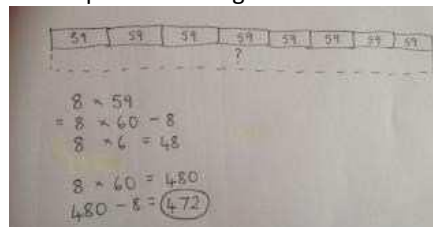
Column multiplication

Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.



Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

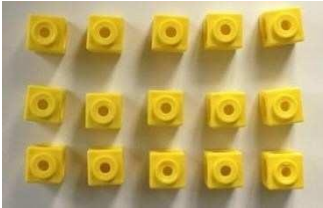
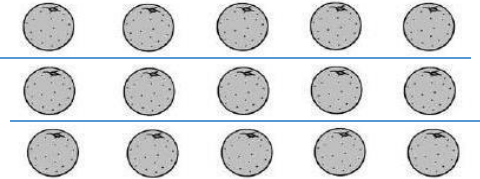
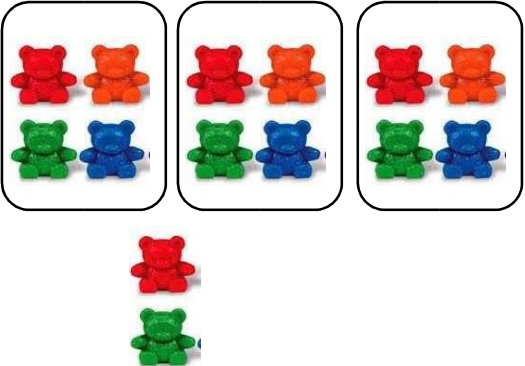
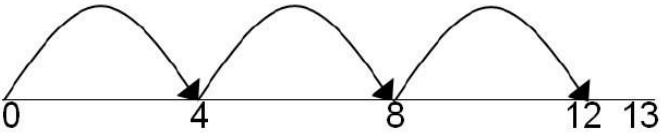

If it helps, children can write out what they are solving next to their answer.

$$\begin{array}{r} 32 \\ \times 24 \\ \hline 8 \quad (4 \times 2) \\ 120 \quad (4 \times 30) \\ 40 \quad (20 \times 2) \\ 600 \quad (20 \times 30) \\ \hline 768 \end{array}$$

$$\begin{array}{r} 7 4 \\ \times 6 3 \\ \hline 1 2 \\ 2 1 0 \\ 2 4 0 \\ + 4 2 0 0 \\ \hline 4 6 6 2 \end{array}$$

This moves to the more compact method.

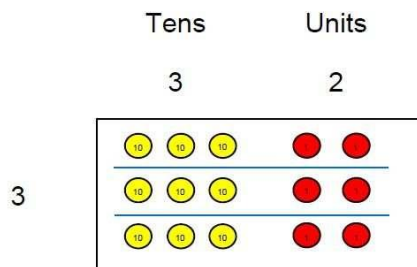
$$\begin{array}{r} 327 \\ \times 53 \\ \hline 981 \quad \leftarrow 327 \times 3 \\ 16350 \quad \leftarrow 327 \times 50 \\ \hline 17331 \end{array}$$

<p>Division within arrays</p>	 <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$</p>	 <p>Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p>	<p>Find the inverse of multiplication and division sentences by creating four linking number sentences.</p> <p>$7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$</p>
<p>Division with a remainder</p>	<p>$14 \div 3 =$ Divide objects between groups and see how much is left over</p> 	<p>Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.</p>  <p>Draw dots and group them to divide an amount and clearly show a remainder.</p> 	<p>Complete written divisions and show the remainder using r.</p> <p>$29 \div 8 = 3 \text{ REMAINDER } 5$</p> <p>↑ ↑ ↑ ↑ dividend divisor quotient remainder</p>

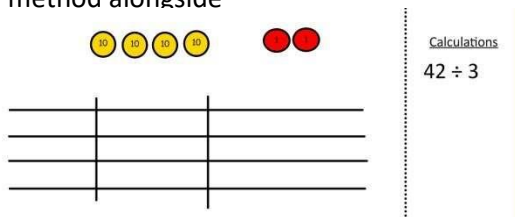
Short division

Find one third of 96.

$$96 \div 3 =$$

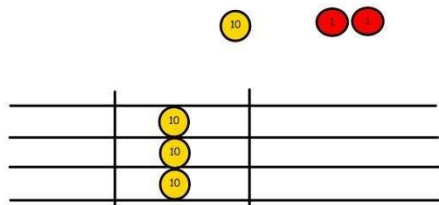


Use place value counters to divide using the bus stop method alongside

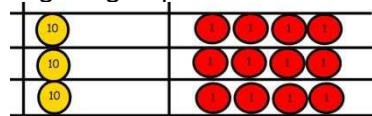


$$42 \div 3 =$$

Start with the biggest place value; share 40 into three groups. Put 1 ten in each group then 1 ten left over.

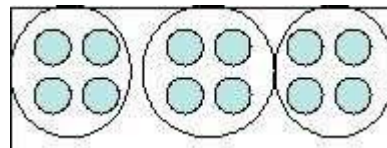


Exchange this ten for ten ones and then share the ones equally among the groups.



Look how much is in 1 group so the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

$$\begin{array}{r} 218 \\ 3 \overline{) 872} \end{array}$$

Move onto divisions with a remainder.

$$\begin{array}{r} 86 \text{ r } 2 \\ 3 \overline{) 432} \end{array}$$

Finally move into decimal places to divide the total accurately.

$$\begin{array}{r} 14.6 \\ 35 \overline{) 511.0} \end{array}$$

Long division

(Partitioning method)

Divide by single digit then progress to dividing by two digit number

Divide :

2

3

74

→

Dividing 7 tens by 3, we get 2 tens, and some extra.

Multiply :

2

3

74

→

3 × 2 tens = 60 tens.

Subtract :

2

3

74

→

Subtracting 6 tens from 7 tens

Bring down :

2

3

74

→

1 ten 4 ones = 14 ones

Repeat or find the Remainder :

2 4

3

74

→

Dividing 14 ones by 3, we get 4 ones and some extra.

2 4

3

74

→

3 × 4 ones = 12 ones.

→

Remainder

Check :

Check your answer:

Dividend = Divisor × Quotient + Remainder

Division of fractions

$\frac{1}{2} \div 3 =$

Half of the pizza divided into three equal parts.

$\frac{1}{2} \div 3 =$

Half of the bar divided into three equal parts.

$\frac{1}{2} \div 3 =$

$\frac{1}{2} \div \frac{3}{1} =$

$\frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$

Times Table Policy

TIMES IT!

Times Tables are at the heart of mental arithmetic, which in itself helps form the basis of a child's understanding and ability when working with number. Once the children have learnt their times tables by heart, they are then able to work far more confidently and efficiently through a wide range of more advanced calculations. At Priestsic Primary School, we believe that through a variety of interactive, visual, engaging and rote learning techniques, most children can achieve the full times table knowledge by the time they enter Year 5.

Reception	Year 1	Year 2	Year 3	Year 4	Year 5 and 6
I can count in steps of 1 I can count in steps of 2 I can count in steps of 10 I can count in steps of 5	I can count in steps of 1 I can count in steps of 2 I can count in steps of 10 I can count in steps of 5	I know my 2 times table and related division facts. I know my 5 times table and related division facts. I know my 10 times table and related division facts. I can count in steps of 3	I know my 3 times table I know my 6 times table I know my 4 times table I know my 8 times table I can count in steps of 4, 6, 8, 50 and 100	I know my 7 times table I know my 9 times table I know my 11 times table I know my 12 times table I can count in steps of 7, 9 and 25	Regular consolidation of all times tables Year 5 – I can count in powers of 10

Rote learning

Times tables will be recited daily. Chant as: 'One times two is two, two times two is four, three times two is six

Also chant as 'one multiplied by two is two, one two is two, one lot of two is two, one group of two is two, the product of one and two is two etc.'

Use your counting stick to carry out this activity.

Display

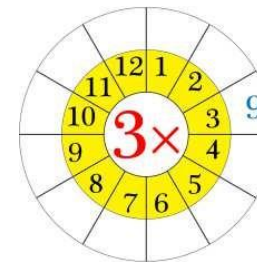
Times tables should be readily available on enable table, for children to use as support and reference.

Year 1: 1, 2, 5 and 10 times tables should be available.



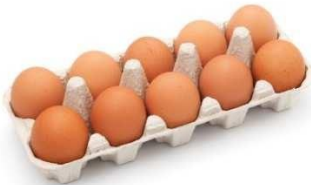

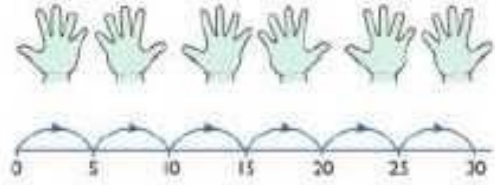
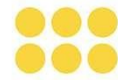
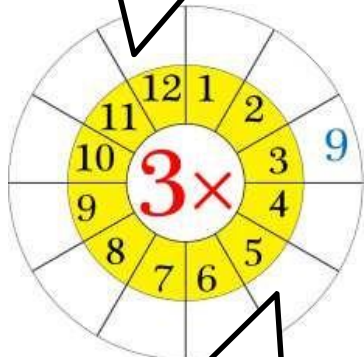
Year 2: 1, 2, 3, 5 and 10 times tables should be available

KS2: All times tables up to 12 x 12 should be available for children.

1 x 1 = 1	2 x 1 = 2	3 x 1 = 3	4 x 1 = 4	5 x 1 = 5
1 x 2 = 2	2 x 2 = 4	3 x 2 = 6	4 x 2 = 8	5 x 2 = 10
1 x 3 = 3	2 x 3 = 6	3 x 3 = 9	4 x 3 = 12	5 x 3 = 15
1 x 4 = 4	2 x 4 = 8	3 x 4 = 12	4 x 4 = 16	5 x 4 = 20
1 x 5 = 5	2 x 5 = 10	3 x 5 = 15	4 x 5 = 20	5 x 5 = 25
1 x 6 = 6	2 x 6 = 12	3 x 6 = 18	4 x 6 = 24	5 x 6 = 30
1 x 7 = 7	2 x 7 = 14	3 x 7 = 21	4 x 7 = 28	5 x 7 = 35
1 x 8 = 8	2 x 8 = 16	3 x 8 = 24	4 x 8 = 32	5 x 8 = 40
1 x 9 = 9	2 x 9 = 18	3 x 9 = 27	4 x 9 = 36	5 x 9 = 45
1 x 10 = 10	2 x 10 = 20	3 x 10 = 30	4 x 10 = 40	5 x 10 = 50
1 x 11 = 11	2 x 11 = 22	3 x 11 = 33	4 x 11 = 44	5 x 11 = 55
1 x 12 = 12	2 x 12 = 24	3 x 12 = 36	4 x 12 = 48	5 x 12 = 60



Process of teaching times tables

Children will be taught the concept of multiplication using practical resources.	Children will progress on to using number lines or pictures.	Children will count in multiple steps.	Children will recite times tables by rote. Links will be made with 'grouping' and division whilst times tables are being taught.																								
Concrete BUILD IT! / USE IT!	Pictorial DRAW IT!	Abstract stage 1 SOLVE IT!	Abstract stage 2 PRACTISE IT!																								
Count in multiples supported by concrete objects in equal groups.   Use real-life arrays or build arrays.  	 Use a number line or pictures to continue support in counting in multiples. <div data-bbox="591 970 1008 1203"><p>What do you notice?</p><p>$3 \times 2 = 6$</p><p>3</p><p>2 {</p></div> <div data-bbox="996 1302 1408 1509"><p>Link multiplication and division facts.</p></div>	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30 Record multiplication number sentences. <div data-bbox="1263 979 1637 1308"><table><tr><td>$1 \times 7 = 7$</td><td>$7 \div 7 = 1$</td></tr><tr><td>$2 \times 7 = 14$</td><td>$14 \div 7 = 2$</td></tr><tr><td>$3 \times 7 = 21$</td><td>$21 \div 7 = 3$</td></tr><tr><td>$4 \times 7 = 28$</td><td>$28 \div 7 = 4$</td></tr><tr><td>$5 \times 7 = 35$</td><td>$35 \div 7 = 5$</td></tr><tr><td>$6 \times 7 = 42$</td><td>$42 \div 7 = 6$</td></tr><tr><td>$7 \times 7 = 49$</td><td>$49 \div 7 = 7$</td></tr><tr><td>$8 \times 7 = 56$</td><td>$56 \div 7 = 8$</td></tr><tr><td>$9 \times 7 = 63$</td><td>$63 \div 7 = 9$</td></tr><tr><td>$10 \times 7 = 70$</td><td>$70 \div 7 = 10$</td></tr><tr><td>$11 \times 7 = 77$</td><td>$77 \div 7 = 11$</td></tr><tr><td>$12 \times 7 = 84$</td><td>$84 \div 7 = 12$</td></tr></table></div>	$1 \times 7 = 7$	$7 \div 7 = 1$	$2 \times 7 = 14$	$14 \div 7 = 2$	$3 \times 7 = 21$	$21 \div 7 = 3$	$4 \times 7 = 28$	$28 \div 7 = 4$	$5 \times 7 = 35$	$35 \div 7 = 5$	$6 \times 7 = 42$	$42 \div 7 = 6$	$7 \times 7 = 49$	$49 \div 7 = 7$	$8 \times 7 = 56$	$56 \div 7 = 8$	$9 \times 7 = 63$	$63 \div 7 = 9$	$10 \times 7 = 70$	$70 \div 7 = 10$	$11 \times 7 = 77$	$77 \div 7 = 11$	$12 \times 7 = 84$	$84 \div 7 = 12$	Recite times tables by rote orally. <div data-bbox="1695 537 2114 1465"><p>3 times 3 equals 9, so 9 divided by 3 equals 3. One third of 9 equals 3.</p><p>If you know 3 times 3 equals 9, what else do you know? 3 x 30 = 90 etc.</p></div>
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DIFFERENT WAYS OF COUNTING				
Single steps	Multiples	Use a rule eg $10 + 1 - 3$	Missing numbers	Odds or evens
Fractions	Units of time	Millilitres/litres	Centimetres/metres	Decimals
Grams/kilograms	Negative numbers / Temperature	Percentages	Ordinals	Money
VISUAL AIDS FOR COUNTING				
Number line	100 square	Counting beads	Bead frame	Objects
Number snake	Number tiles	Pocket number line	Real money, large money or magnetic money	Shapes eg count sides
Counting stick	Whiteboards making own visual prompt	Objects (real life)	Base 10 Hundreds, tens, units	Groups of straws
Real life packaging showing arrays eg egg boxes, biscuit packets	Wrapping paper, wall paper etc. to count number of shapes	Number track	Counting bead string	Tape measure or metre stick
Clocks	Measuring jugs	Thermometer	Bead frame/abacus	Calculator
Pictures	Fingers	Interactive whiteboard	Multilink/buttons etc.	Number cards
REHEARSE IT!				
<p>Rehearsing old skills: Children need to rehearse skills already taught to lead them to MASTERY. The objectives will depend on your year group; however, it is important to keep old skills alive. Remember to present the old skills in a variety of ways eg. Venn diagrams, Carroll diagrams, pictograms, tables, < and > signs, missing information, etc.</p>				

REASON IT!

<p>There is a huge emphasis on reasoning in maths lessons. Children need opportunities to justify and explain their knowledge. Ensure you are using: NCETM reasoning questions NCETM mastery documents NRICH tasks Deeper Learning Stickers Groups Work</p>			
Odd one out	Would you rather have ... ?	Find the mistake.	What is the same and what is different?
True or false?	Here is the answer, explain how it was worked out.	Always, sometimes, never	Give me a silly answer to this problem. What makes it silly?
Tell me about this...	Prove/disprove this statement.	Convince me that ...	What if....?
<p>Give me a hard and easy example of a calculation you could do with these numbers.</p> <p>Give me a hard and easy example of a five-digit calculation.</p> <p>Give me a hard and easy example of a question you could ask about this graph/pie chart etc.</p>	What do you notice?	How are these linked?	<p>If you know this fact, what else do you know? Eg. If you know: $4 + 6 = 10$ You know: $40 + 60 = 100$ $100 - 40 = 60$ The sum of 6 and 4 is 10. $4000 + 6000 = 10,000$ $100,000 - 60,000 = 40,000$ If it is 6 o'clock now, in 4 hours it will be 10 o'clock.</p>

RECALL IT!

<p>Rapid recalling of key facts is important in developing fluency and MASTERY. As children recall facts, deepen their knowledge by reasoning in context eg. When recalling number, bonds totalling 100: 'tell me two lengths that together make one metre.'</p>			
Recall number bonds	Recall addition / subtraction facts	Recall multiplication / division facts	Recall fraction, decimal, percentage equivalents
Recall shape names and properties	Recall time related facts	Recall measurement facts	

SAY IT!

Build mathematical vocabulary into every lesson.

Encourage children to speak in full sentences when giving responses.

Use Stem sentences as a model

Taboo – describe this word without saying it	How many words can you link to this word?	Match the word and its meaning.	Use a picture. How many mathematical words can you use?
Which of these words is the odd one out?	Write the definition of this word for someone who does not understand what it means.	Which word do these words link to?	Word of the day – use this word as many times in the day as possible (in context of course!)
Can you say a sentence which links these two words?	Tell me everything you can about this word.	Can you draw a picture to explain this word?	Hangman